

Combining Kinematics + Dynamics

You need to know everything about acceleration + displacement:

$$\begin{array}{l}
 a = \frac{\Delta v}{\Delta t} \quad (\Delta v = v_2 - v_1) \\
 v_{ave} = \frac{\Delta d}{\Delta t} \quad (v_{ave} = \frac{v_1 + v_2}{2})
 \end{array}
 \left. \vphantom{\begin{array}{l} a \\ v_{ave} \end{array}} \right\} \text{constant acceleration}$$

Maybe Useful Equations

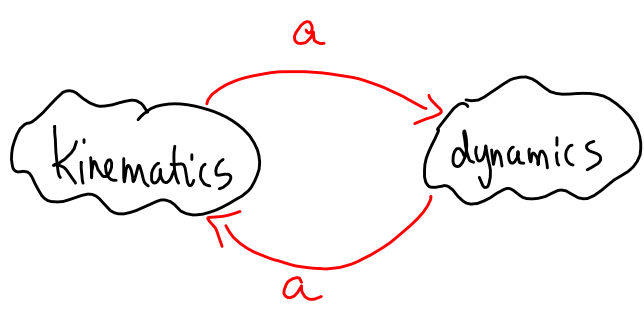
- ① $\Delta d = v_1 t + \frac{1}{2} a t^2$
- ② $\Delta d = v_2 t - \frac{1}{2} a t^2$
- ③ $v_2^2 = v_1^2 + 2 a \Delta d$

You also need to know about forces:

Weight: $F_g = mg$
 friction: $F_f = \mu F_N \quad \leftarrow \text{FBD}$

Newton's Laws

- ① Law of Inertia
- ② $\vec{F}_{net} = m\vec{a}$ (FBD)
- ③ ?



mp/165



$$m = 9.1 \times 10^{-31} \text{ kg}$$

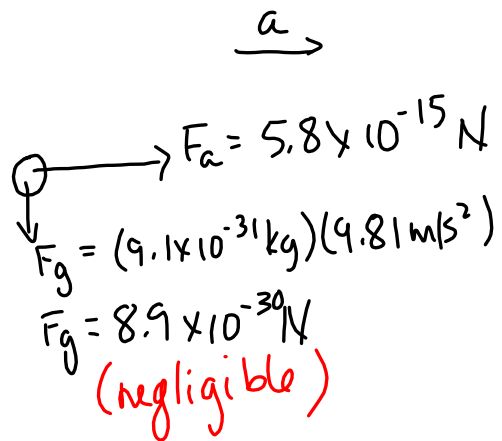
$$F_a = 5.8 \times 10^{-15} \text{ N}$$

$$v_1 = 0$$

$$\Delta d = 3.5 \text{ mm}$$

$$v_2 = ?$$

Draw a FBD:



Find the acceleration:

$$\vec{F}_{\text{net}} = m\vec{a}$$

$$F_a = ma$$

$$a = \frac{F_a}{m}$$

$$a = \frac{5.8 \times 10^{-15} \text{ N}}{9.1 \times 10^{-31} \text{ kg}}$$

$$a = 6.4 \times 10^{15} \text{ m/s}^2$$

$\leftarrow \text{kg} \cdot \text{m/s}^2$

Now find v_2 :

$$v_2^2 = \cancel{v_1}^2 + 2a\Delta d$$

$$v_2^2 = 2(6.4 \times 10^{15} \text{ m/s}^2)(3.5 \times 10^{-3} \text{ m})$$

$$v_2^2 = 4.4615 \times 10^{13} \text{ m}^2/\text{s}^2$$

$$v_2 = 6.7 \times 10^6 \text{ m/s}$$

MP/166

$$\vec{F}_a = 9.50 \text{ N [S]}$$

$$m = 20.0 \text{ kg}$$

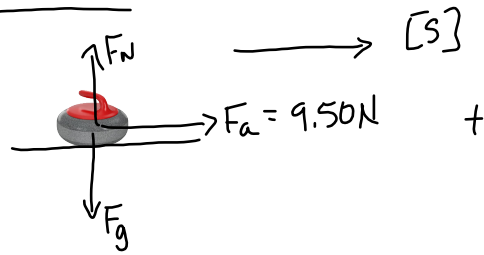
$$v_i = 0$$

$$\Delta t = 1.86 \text{ s}$$

a) $\vec{a} = ?$

b) $\vec{v}_2 = ?$

Draw a FBD:



Find acceleration:

$$\vec{F}_{net} = m\vec{a}$$

$$\vec{F}_a = m a$$

$$a = \frac{\vec{F}_a}{m}$$

$$a = \frac{9.50 \text{ N}}{20.0 \text{ kg}}$$

$$a = 0.475 \text{ m/s}^2$$

$$\vec{a} = 0.475 \text{ m/s}^2 \text{ [S]}$$

b) find v_2 :

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

$$\vec{a} = \frac{\vec{v}_2 - \vec{v}_1}{\Delta t}$$

$$\vec{v}_2 = \vec{v}_1 + \vec{a} \Delta t$$

$$\vec{v}_2 = (0.475 \text{ m/s}^2 \text{ [S]}) (1.86 \text{ s})$$

$$\vec{v}_2 = 0.884 \text{ m/s [S]}$$

TO DO

① PP/168

FBD for car braking:

