

Chapter 5 - Statistical Reasoning

Measures of Central Tendency

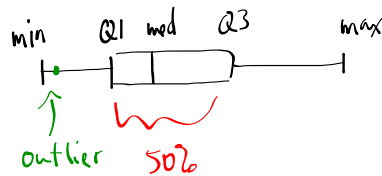
mean (average) \rightarrow (sum of all values) \div n

median \rightarrow middle value when sorted ascending or descending.

mode \rightarrow most frequent value.

range \rightarrow how spread out the data is (min, max)

outlier \rightarrow a value that is very different from the other values



dispersion \rightarrow how spread out the data is (the range is a measure of the dispersion)

§5-1 Exploring Data

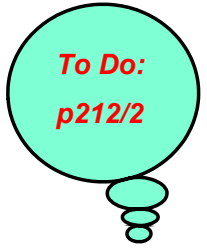
L1	L2	L3	1
5.4	6.8		
5.7	5.7		
5.7	5.9		
5.7	4.8		
5.7	5.5		
5.8	5.8		
5.8	5.6		

L1(10) = 5.1
 3 occurrences
 So mode is 5.7

	Brand X	Brand Y
mode	5.7 yrs	
mean (\bar{x})	5.74 yrs	
median	5.75 yrs	
range	(3.1, 8.2)	

```

mean
1-Var Stats
x̄=5.743333333
Σx=172.3
Σx²=1034.37
Sx=1.242823075
sx=1.221933804
n=30
1-Var Stats
n=30
minX=3.1
Q1=5
Med=5.75 median
Q3=6.4
maxX=8.2
    
```



§5-2 Frequency Tables, Histograms + Frequency Polygons

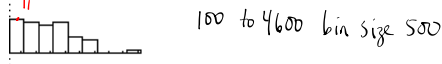
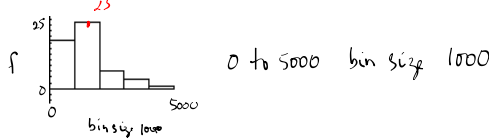
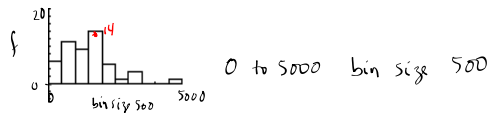
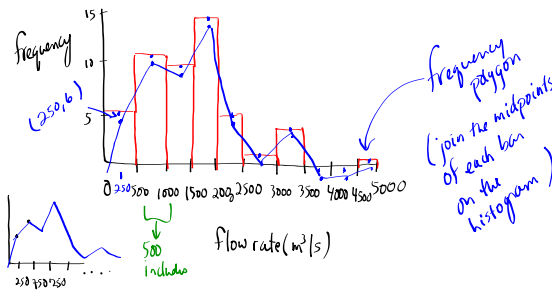
Frequency Table

min = 159 } 0-5000
 max = 4587 } 10 groups

flowrate (m ³ /s)	Tally	Frequency
0 - 500	### 1	6
500 - 1000		11
includes 1000 → 1000 - 500 ← doesn't include		9
1500 - 2000		14
2000 - 2500		5
2500 - 3000		1
3000 - 3500		3 floods
3500 - 4000		0
4000 - 4500		0
4500 - 5000		1 floods

Bin size → 500

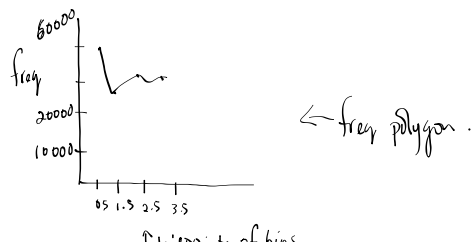
Histogram (use the frequency table)



TO DO

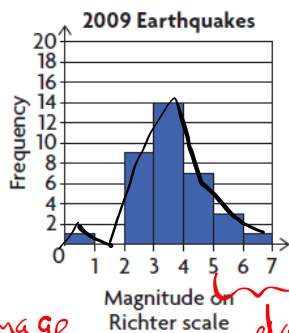
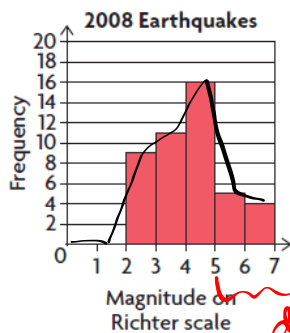
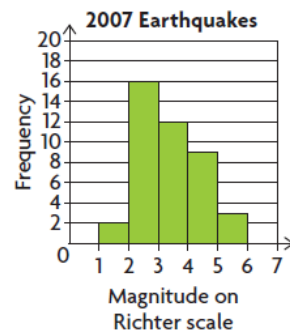
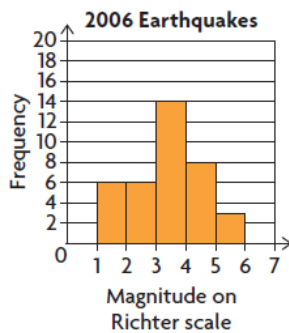
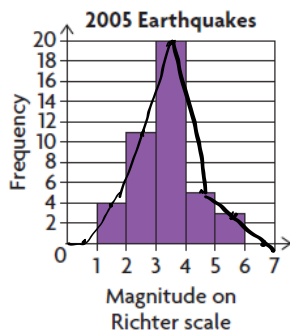
C4U (p21) - do by hand

Practise (p22) - do by hand (check with calc)



EXAMPLE 2 Comparing data using histograms

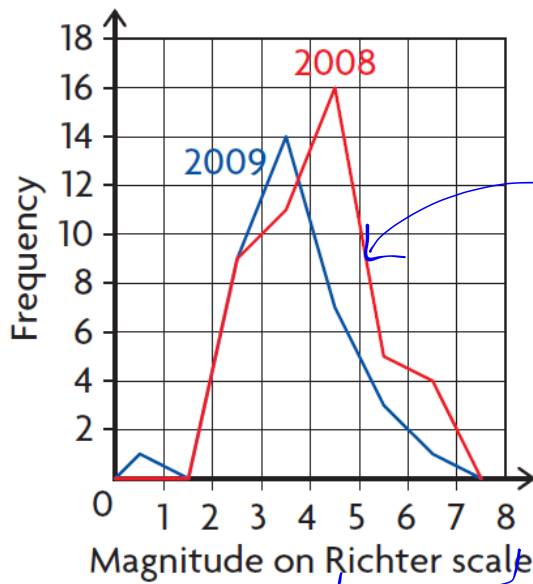
The magnitude of an earthquake is measured using the Richter scale. Examine the histograms for the frequency of earthquake magnitudes in Canada from 2005 to 2009. Which of these years could have had the most damage from earthquakes?



damage *damage*

National Research Council Canada

Both 2008 and 2009 had the strongest earthquakes, registering from 6.0 to 6.9 on the Richter scale.



frequency polygon shows more damage (>5) for 2008

To Do:
p222/3-5

The number of earthquakes in the three highest magnitude intervals was greater in 2008 than in 2009, so 2008 could have had the most damage from earthquakes.

I examined histograms of earthquakes with magnitude greater than 6.0. Both 2008 and 2009 had the most earthquakes in the 6.0 to 6.9 interval, which registered the most damage.

I decided to use a frequency polygon to compare the two years.

I compared the two years.

§5-3 Standard Deviation (p226)

<u>TEST</u>	<u>Class A</u>	<u>Class B</u>	
1	94%	84%	
2	56%	77%	
3	89%	76%	
4	67%	81%	
5	84%	74%	
(mean) \bar{x}	78%	78%	
range	min	56%	74%
	max	94%	84%
range spread	38%	10%	

Class B has more consistent marks since they are closer together and less spread out. Both classes have about the same mean.

p226

Player	Field Goal Percent in Last 10 Basketball Games									
Anna	36	41	43	39	45	27	40	37	31	28
Patrice	36	39	36	38	35	37	35	36	38	34
Morgan	34	41	38	37	48	19	33	43	21	44
Paige	34	35	33	35	33	34	33	35	34	33
Star	41	33	39	36	38	36	29	34	38	39

x̄ = ?
33.9

? How can the coach use the data to determine which player should be substituted into the game?

A. Which player seems to be the most consistent shooter? Explain.

B. Analyze the data for Paige using a table like the one shown on the next page. Determine the mean of the data, \bar{x} , for Paige, and record this value in the first column.

p226
x̄ = 33.9

Paige's Field Goal (%)	Deviation (x - x̄)	Square of Deviation (x - x̄)²
34	34 - 33.9 = 0.1	0.01
35	1.1	1.21
33	-0.9	0.81
35	1.1	1.21
33	-0.9	0.81
34	0.1	0.01
33	-0.9	0.81
35	1.1	1.21
34	0.1	0.01
33	-0.9	0.81
		6.90

Σ

little sigma (standard deviation)

big sigma (means sum)

$$\sigma = \sqrt{\frac{\sum(x - \bar{x})^2}{n}}$$

mean

```
1-Var Stats
x̄ = 33.9
Σx = 339
Σx² = 11499
Sx = .8755950358
σx = .8306623863
n = 10
```

stand. dev.

$$\sigma = \sqrt{0.69}$$

$$\sigma = 0.83$$

mean:

$$\bar{x} = \frac{\sum x}{n}$$

Standard deviation tells you how clustered the data is about the mean. The smaller the value the closer the data is to the mean.

Standard deviation:

$$\sigma = \sqrt{\frac{\sum(x - \bar{x})^2}{n}}$$

	\bar{x}	σ
Anna		
Patrice		
Morgan		
Paige	33.9	0.83
Star		

Example 1 (p228)

of his task is to unload delivery trucks. He wondered about the accuracy of the mass measurements given on two cartons that contained sunflower seeds. He decided to measure the masses of the 20 bags in the two cartons. One carton contained 227 g bags, and the other carton contained 454 g bags.

L1 Masses of 227 g Bags (g)				L2 Masses of 454 g Bags (g)			
228	220	233	227	458	445	457	458
230	227	221	229	452	457	445	452
224	235	224	231	463	455	451	460
226	232	218	218	455	453	456	459
229	232	236	223	451	455	456	450

How can measures of dispersion be used to determine if the accuracy of measurement is the same for both bag sizes?

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	<u>227g bags</u>	<u>454g bags</u>
min	218 g	445 g
max	236 g	463 g
mean (\bar{x})	227.15 g	454.4 g
st. dev (σ)	5.227 g	4.498 g

↑
more consistent

* Both samples have the range, but the 454g bags were more consistent (less spread out).

* Standard deviation is a better measure of the dispersion of data as opposed to the range.

To DO

- ① Finish the BBall example with calculator.
- ② CU(p233) / #1 (do by hand)
- ③ Practice (p233) / 5 - 8 (with calc)
- ④ MidChapter Review (p238-240 / 1-5)