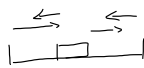


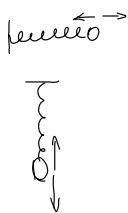
Oscillatory Motion

Glider on airtrack



oscillatory but not simple harmonic motion
(no net force, except at ends)

Bob on a spring:



Pendulum:



Tube of water:



All examples of simple harmonic motion (SHM)

There is an unbalanced or net force acting on the object when the object is displaced from its equilibrium position.

Recall Hooke's law:

$$F = -kx$$

The unbalanced force in SHM is proportional to the displacement from the equilibrium position.

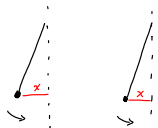
Period (T) $\Rightarrow T = \frac{\text{time (s)}}{\text{cycles}}$
 Frequency (f) $\Rightarrow f = \frac{\text{cycles}}{\text{time (Hz)}}$
 Period + frequency are reciprocals
 $T = \frac{1}{f}$ and $f = \frac{1}{T}$

$$\text{kHz} = 10^3 \text{ Hz}$$

$$\text{MHz} = 10^6 \text{ Hz}$$

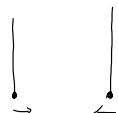
$$\text{GHz} = 10^9 \text{ Hz}$$

Phase:



in phase.

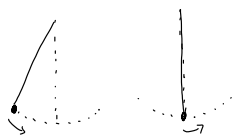
Phase Difference:
(out of phase)



out of phase



in opposite phase



The second pendulum leads the first and is a quarter of a period ahead

Phase difference is $\frac{T}{4}$

Example

The atoms in an O_2 molecule oscillate with a frequency of $4.0 \times 10^{14} \text{ Hz}$. What is the period of oscillation?

$$T = \frac{1}{f}$$

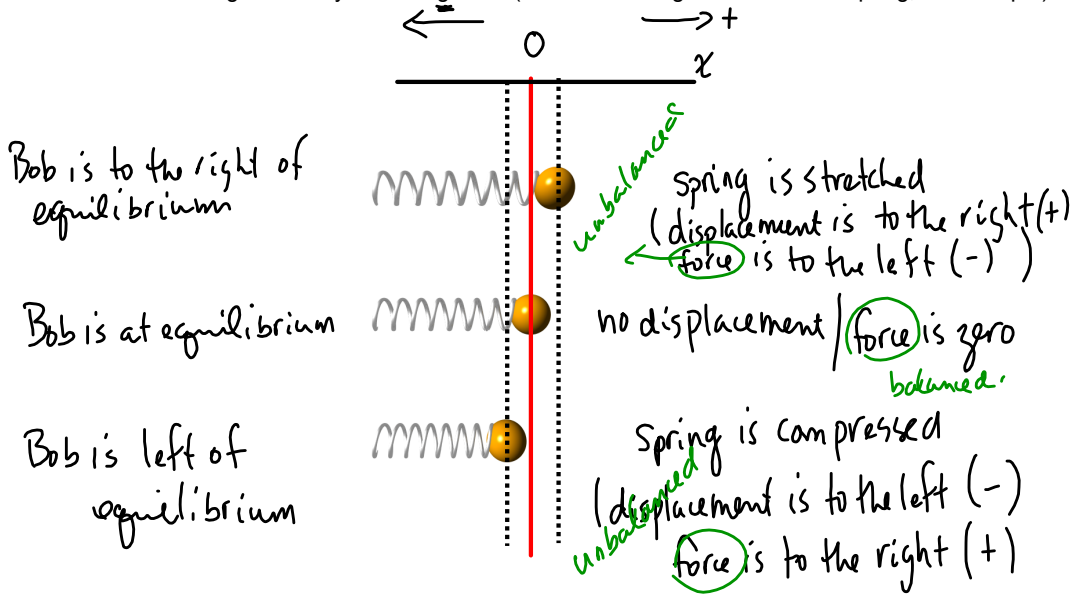
$$T = \frac{1}{4.0 \times 10^{14} \text{ s}^{-1}}$$

$$T = 2.5 \times 10^{-15} \text{ s}$$

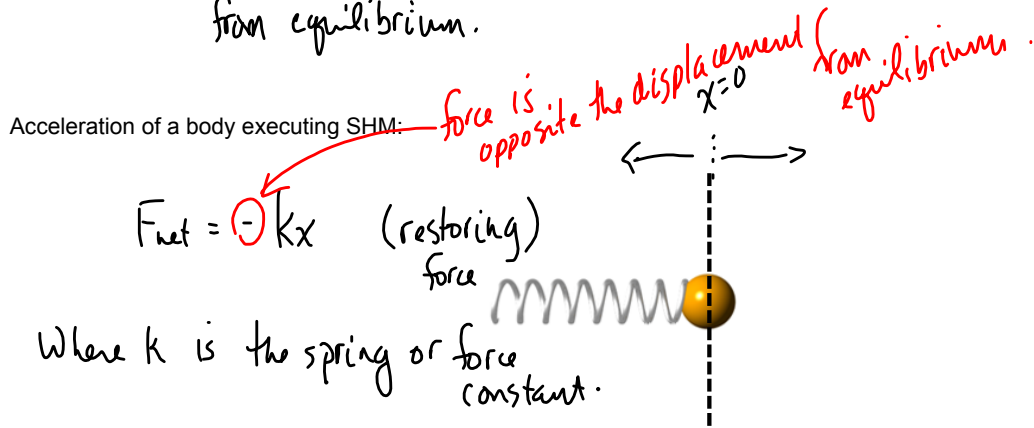


So what is simple harmonic motion and what is the defining equation?

Consider the force acting on a body executing SHM (a bob oscillating on a horizontal spring, for example):



Recall Hooke's Law \rightarrow force is proportional to the displacement from equilibrium.



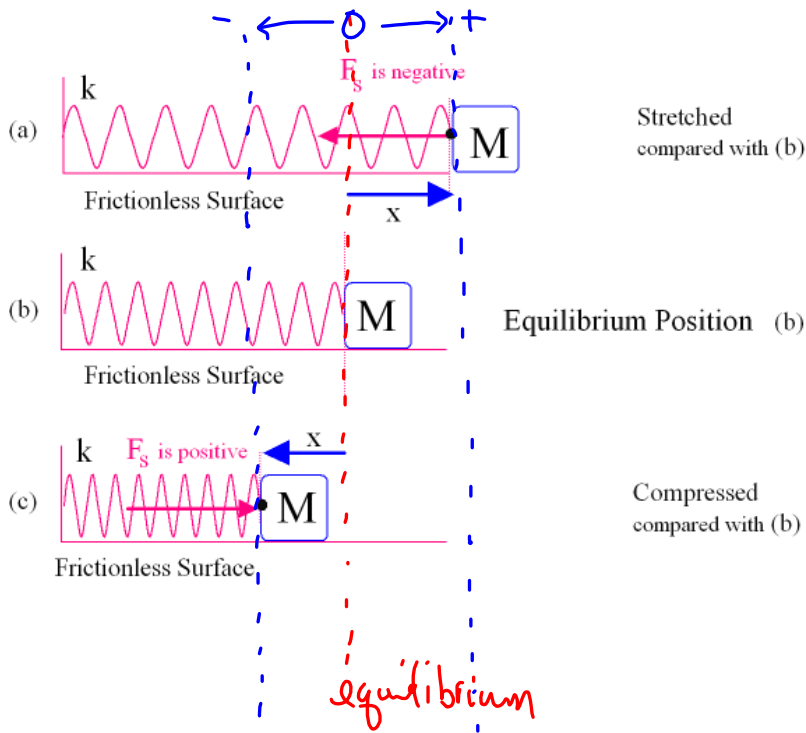
Recall Newton's 2nd Law: $F_{net} = ma$ where m is the mass of the bob and a is the acceleration.

$$ma = -kx$$

$$a = -\frac{k}{m}x$$

$$a \propto -x$$

\leftarrow acceleration is directly proportional to the displacement and is in the opposite direction to the displacement. (i.e. towards the equilibrium)

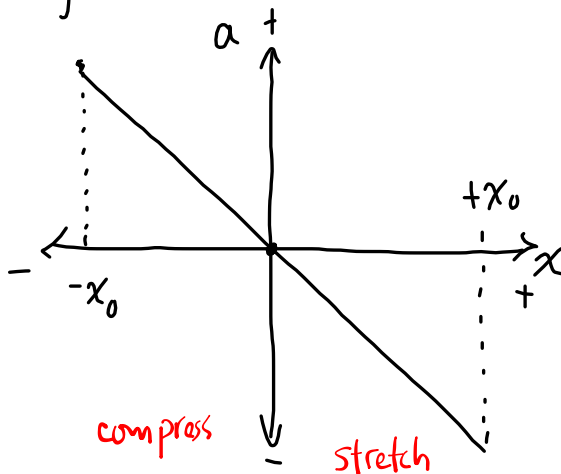


x is positive (to right)
 F is negative (to left)
 a is negative (to left)

$x = 0, F = 0, a = 0$

x is negative (to left)
 F is positive (to right)
 a is positive (to right)

A graph of acceleration vs extension



The graph is linear since the acceleration is directly proportional to x (displacement)

x_0 is the max extension
 x is any extension

Definition of Simple Harmonic Motion

SHM is oscillatory motion in which the acceleration is:

- proportional to the displacement and
- is directed toward the equilibrium.

Since the acceleration is directly proportional and in the opposite direction we can write a proportionality statement:

$$a \propto -x$$

$$a = -\omega^2 x$$

← Defining Equation for SHM

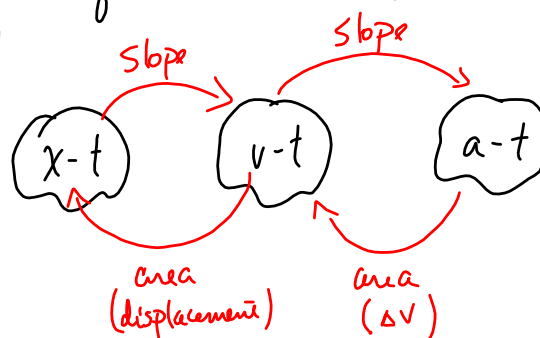
Where x is the displacement
 a is the acceleration
 ω^2 is the proportionality constant

ω is called the angular frequency of the oscillation
 Units: s^{-1} or $\text{rad } s^{-1}$

Note: cannot

- We solve kinematics problems involving SHM using our "suvat" equations because the acceleration is NOT constant during SHM. The acceleration is constantly changing!

- the significance of the kinematics graphs ($x-t$, $v-t$, $a-t$) are still valid



To show that an oscillatory motion IS simple harmonic motion, then we must show that:

$$a \propto -x$$

Consider the pendulum:
It has oscillatory motion, but is it SHM??

restoring force

$$F_{\text{net}} = mg \sin \theta$$

$$F_{\text{net}} = mg \frac{x}{l}$$

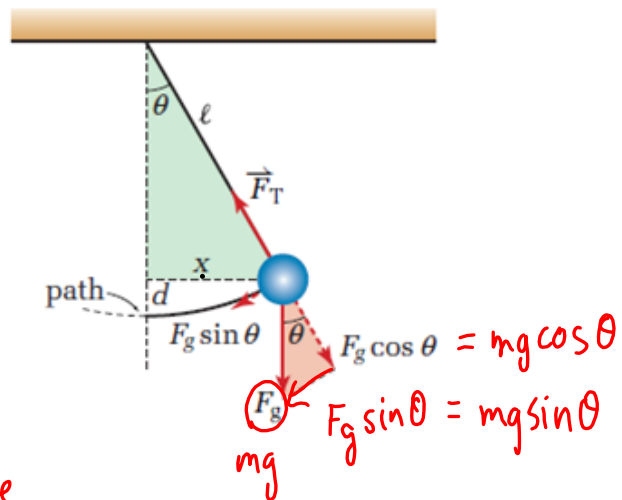
$$ma = \frac{mg}{l} x$$

$$a = -\frac{g}{l} x$$

insert -ve
since acc is opp x

$$\text{so: } a \propto -x$$

and the pendulum exhibits SHM



Graphs of Simple Harmonic Motion

