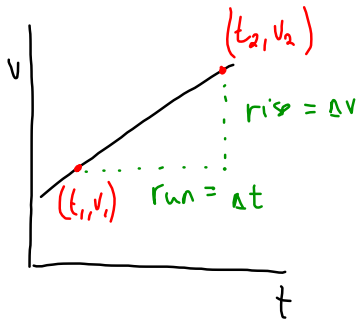


Velocity-Time Graphs + Acceleration

Constant Acceleration



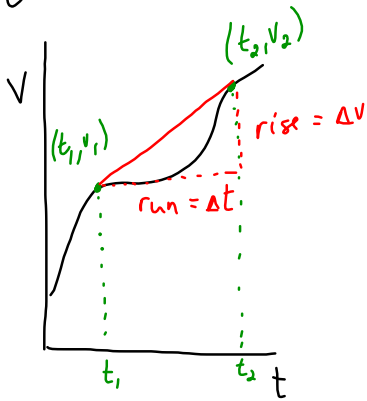
slope = $\frac{\text{rise}}{\text{run}}$

slope = $\frac{\Delta v}{\Delta t}$

From INVS we know that the slope on a v-t graph is acceleration

$\therefore a = \frac{\Delta v}{\Delta t}$

Non-Constant Acceleration

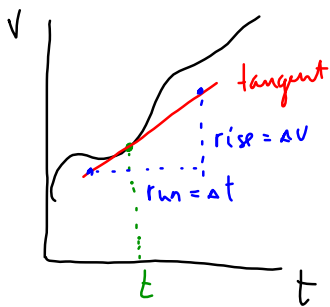


slope = $\frac{\text{rise}}{\text{run}}$

slope = $\frac{\Delta v}{\Delta t}$

Average acceleration is the slope of the line between two points on the v-t graph.

$a_{\text{ave}} = \frac{\Delta v}{\Delta t}$

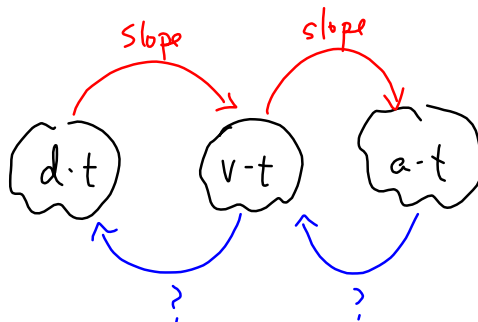


slope = $\frac{\text{rise}}{\text{run}}$

slope = $\frac{\Delta v}{\Delta t}$

Instantaneous acceleration is the slope of the tangent at time t on a v-t graph.

$a_{\text{inst}} = \frac{\Delta v}{\Delta t}$



The acceleration Equation

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t} \quad \text{acceleration is a vector!}$$

where \vec{a} is the acceleration (m/s^2)

$\Delta \vec{v}$ is the change in velocity (m/s)

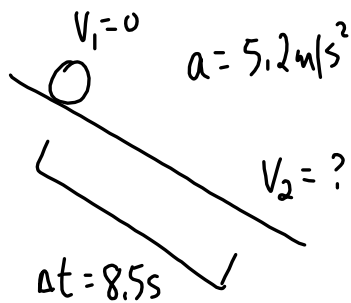
$$\Delta \vec{v} = \vec{v}_2 - \vec{v}_1$$

Δt is the time interval (s)

units: $\frac{\text{m/s}}{\text{s}} = \text{m/s/s}$

$$\frac{\text{m}}{\text{s}} \div \text{s} = \frac{\text{m}}{\text{s}} \cdot \frac{1}{\text{s}} = \frac{\text{m}}{\text{s}^2} \quad \text{or } \text{mS}^{-2}$$

MP/77



G

$$\vec{v}_1 = 0$$

$$\vec{a} = 5.2 \text{ m/s}^2 \text{ [downhill]}$$

$$\Delta t = 8.5 \text{ s} \quad \rightarrow 5.2 \text{ m/s/s}$$

R

$$\vec{v}_2 = ?$$

A

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

$$\vec{a} = \frac{\vec{v}_2 - \vec{v}_1}{\Delta t}$$

$$\vec{a} \Delta t = \vec{v}_2 - \vec{v}_1$$

$$\vec{v}_2 = \vec{v}_1 + \vec{a} \Delta t$$

units: $\frac{\text{m}}{\text{s}^2} \cdot \frac{\text{s}}{1} = \frac{\text{m}}{\text{s}}$

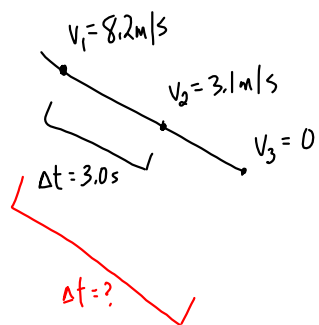
S

$$\vec{v}_2 = 0 \text{ m/s} + (5.2 \text{ m/s}^2 \text{ [downhill]}) (8.5 \text{ s})$$

$$\vec{v}_2 = 44 \text{ m/s [downhill]}$$

P [The velocity of the boulder will be 44 m/s [downhill] after 8.5 s.]

MP/78



Find the acceleration during the first 3.0s.

$$\vec{v}_1 = 8.2 \text{ m/s [downhill]}$$

$$\vec{v}_2 = 3.1 \text{ m/s [downhill]}$$

$$\Delta t = 3.0 \text{ s}$$

$$a = ?$$

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

$$\vec{a} = \frac{\vec{v}_2 - \vec{v}_1}{\Delta t}$$

$$\vec{a} = \frac{3.1 \text{ m/s [downhill]} - 8.2 \text{ m/s [downhill]}}{3.0 \text{ s}}$$

$$\vec{a} = \frac{-5.1 \text{ m/s [downhill]}}{3.0 \text{ s}}$$

$$\vec{a} = -1.7 \text{ m/s}^2 \text{ [downhill]}$$

Now find Δt for whole trip:

$$\vec{v}_1 = 8.2 \text{ m/s [downhill]}$$

$$\vec{v}_2 = 0 \text{ m/s}$$

$$\vec{a} = -1.7 \text{ m/s}^2 \text{ [downhill]}$$

$$\Delta t = ??$$

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

$$\vec{a} \Delta t = \Delta \vec{v}$$

$$\Delta t = \frac{\Delta \vec{v}}{\vec{a}}$$

$$\Delta t = \frac{\vec{v}_2 - \vec{v}_1}{\vec{a}}$$

$$\Delta t = \frac{0 \text{ m/s} - 8.2 \text{ m/s [downhill]}}{-1.7 \text{ m/s}^2 \text{ [downhill]}}$$

$$\Delta t = \frac{-8.2 \text{ m/s [downhill]}}{-1.7 \text{ m/s}^2 \text{ [downhill]}} \leftarrow \text{directions must match}$$

$$\Delta t = 4.8 \text{ s}$$

units: $\frac{\text{m/s}}{\text{m/s}^2}$

$$\frac{\text{m}}{\text{s}} \div \frac{\text{m}}{\text{s}^2} = \frac{\text{m}}{\text{s}} \cdot \frac{\text{s}^2}{\text{m}} = \text{s}$$

The skier came to a stop
4.8 s after falling.

TO DO

• Read over § 2-4 (p61-64) and p74-77

• PP/80