

The unified mass unit is defined as $\frac{1}{12}$ th of the mass of a single neutral atom of the isotope carbon-12 in its ground state.

↳ needs be in the ground state
since any energy is equivalent to mass and the mass is significant at the nuclear level.

Example 50kg object $\Delta h = 3m$ so the potential energy

$$\begin{aligned} \text{is } E_p &= mgh \\ E_p &= 850J \end{aligned}$$

$$E = mc^2$$

$$m = \frac{E}{c^2}$$

$$m = \frac{850J}{(3.00 \times 10^8 \text{ m/s})^2}$$

$$m = 9 \times 10^{-15} \text{ kg}$$

this mass equivalence is insignificant compared to the object.

Example What is the mass equivalence for an energy change of 5eV (an energy associated with electrons)

$$m = \frac{E}{c^2}$$

$$m = \frac{(5eV)(1.6 \times 10^{-19} \text{ J eV}^{-1})}{(3.0 \times 10^8 \text{ m/s}^{-1})^2}$$

$$m \approx 10^{-35} \text{ kg}$$

← not really that significant (compare to mass of an atom)

Example: What is the mass equivalence for 5MeV (nuclear reaction)?

$$m = \frac{(5 \times 10^6 \text{ eV})(1.6 \times 10^{-19} \text{ J eV}^{-1})}{(3.0 \times 10^8 \text{ m/s}^{-1})^2}$$

must
more
significant →

$$m \approx 10^{-29} \text{ kg}$$

in a total mass of $\approx 10^{-26} \text{ kg}$

* ONLY in nuclear reactions that the mass change is large enough to be detectable.

Mass Defect

- energy is required to separate the nucleus into its nucleons
- separated nucleons have more potential energy \Rightarrow \therefore **more mass**.
- difference in the mass of the separated nucleons and the bound nucleons (nucleus) is called the mass defect.

mass defect (Δm) \rightarrow the mass of a nucleus is always less than the total mass of its constituent nucleons and the difference in mass is called the mass defect.

$$\Delta m = Z m_p + N m_n - m_{\text{nucleus}}$$

units: kg more commonly $\text{MeV}c^{-2}$

Binding Energy

- add energy to separate the nucleons, and energy is released when the nucleons are brought together to form the nucleus.

The binding energy E_B of a nucleus is the minimum energy to completely separate the nucleus into its component nucleons.

units: MeV

$$E_B = \Delta m c^2$$

\uparrow
mass defect

When a nucleus is separated into its component nucleons, an amount of energy, E_B is required and the potential energy of the system increases by E_B .

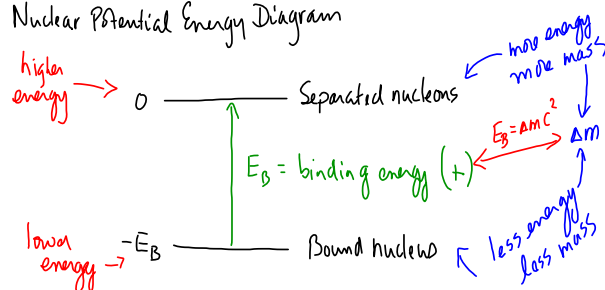
Binding Energy per Nucleon

The binding energy per nucleon of a nucleus is the binding energy of the nucleus divided by the # of nucleons in the nucleus.

$$\frac{E_B}{A} \quad \left. \vphantom{\frac{E_B}{A}} \right\} \text{binding energy per nucleon.}$$

units: "MeV per nucleon"

Nuclear Potential Energy Diagram



Example

$$\left. \begin{array}{l} m_p = 1.0073u \\ m_n = 1.0086u \end{array} \right\} \leftarrow \text{greater than } \frac{1}{12} \text{th of } C^{12}$$

$$m_e = 0.00055u$$

The masses of the individual nucleons are greater than $\frac{1}{12}$ since they are separated and have more potential energy which means more mass.

$$\Delta m = 6m_p + 6m_n - 12u \quad \leftarrow \text{mass of } C^{12} \text{ is EXACTLY } 12u$$

$$\Delta m = 6(1.0073u) + 6(1.0086u) - 12u$$

$$\Delta m = 6.0438u + 6.0516u - 12u$$

$$\Delta m = 12.0954u - 12u$$

$$\Delta m = 0.0954u$$

$$\Delta m = 0.0954u \left(1.661 \times 10^{-27} \frac{\text{kg}}{u} \right)$$

$$\Delta m = 1.5846 \times 10^{-28} \text{ kg}$$

$$E_B = \Delta m c^2$$

$$E_B = (1.5846 \times 10^{-28} \text{ kg}) (3.00 \times 10^8 \text{ m/s})^2 \left(\frac{1 \text{ eV}}{1.6 \times 10^{-19} \text{ J}} \right)$$

$$E_B = 89.1 \text{ MeV}$$

$$\therefore \frac{E_B}{A} = \frac{89.1 \text{ MeV}}{12 \text{ nucleons}}$$

$$= 7.43 \text{ MeV per nucleon}$$

Example

$$1u = 1.661 \times 10^{-27} \text{ kg} = 931.5 \text{ MeV } c^{-2}$$

$$m_p = 1.673 \times 10^{-27} \text{ kg} = 1.007276u = 938 \text{ MeV } c^{-2}$$

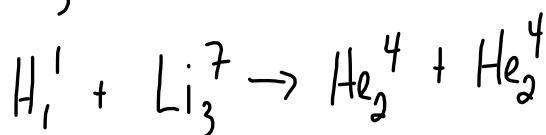
$$m_n = 1.675 \times 10^{-27} \text{ kg} = 1.008665u = 940 \text{ MeV } c^{-2}$$

Use the data to complete the following chart:

	<u>Nucleus</u>	<u>Nuclear mass</u>	Δm	E_B	<u>Binding energy per nucleon</u>
Deuteron	H_1^2	$3.345 \times 10^{-27} \text{ kg}$	↓	↓	0.8 MeV
Nitrogen	N_7^{14}	13,9992u			7.5 MeV
Iron	Fe_{26}^{56}	52,09 GeV c^{-2}			8.9 MeV
Uranium	U_{92}^{238}	$3.953 \times 10^{-25} \text{ kg}$			7.5 MeV

Example

Consider the following nuclear reaction:



Use the data to show 17.3 MeV of energy is released in this reaction. (i.e. exothermic)

mass

$$H^1 = 1.00728u$$

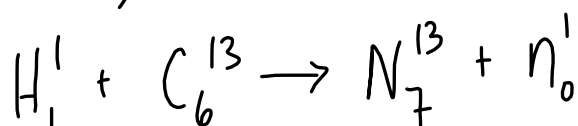
$$Li^7 = 7.01435u$$

$$He^4 = 4.00151u$$

$$m = 931.5 \text{ MeV } c^{-2}$$

Example

Consider the following nuclear reaction:



Use the data to show that 3.0 MeV of energy is required for the reaction to proceed

mass

$$H^1 = 1.00728u$$

$$C^{13} = 13.00006u$$

$$N^{13} = 13.00190u$$

$$n = 1.00866u$$

$$m = 931.5 \text{ MeV } c^{-2}$$