

Conservation of Energy:

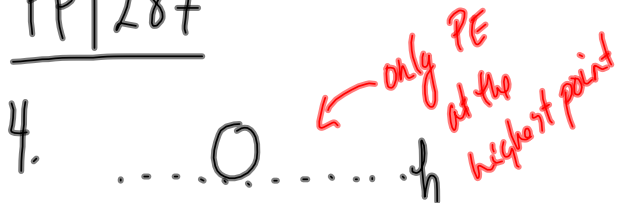
Law of conservation of Mechanical Energy

$$E_{\text{total}} = E'_{\text{total}}$$

(before) (after)

$$E_g + E_k + E_e = E'_g + E'_k + E'_e$$

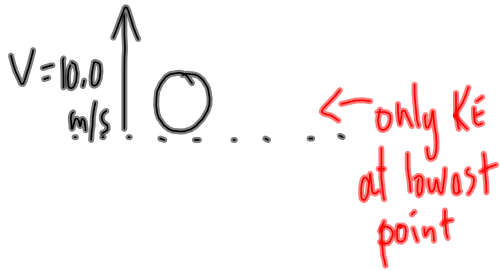
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$$E_{\text{total}} = E'_{\text{total}}$$

(lowest) (highest)

$$0 E_g + E_k = E'_g + E'_k 0$$



$$\frac{1}{2} m v^2 = mgh$$

$$h = \frac{v^2}{2g}$$

Using Kinematics:

$$v_1 = 10.0 \text{ m/s}$$

$$v_2 = 0$$

$$a = -9.8 \text{ m/s}^2$$

$$ad = ?$$

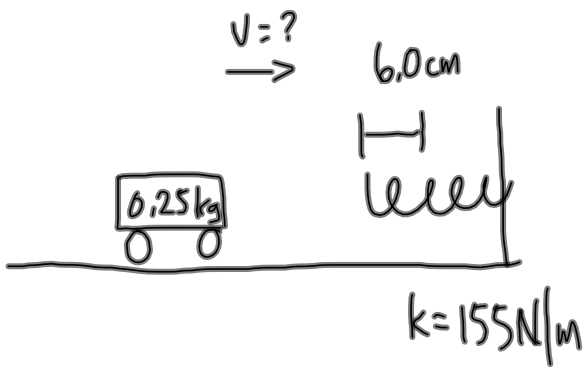
$$v_2^2 = v_1^2 + 2ad$$

$$h = \frac{(10.0 \text{ m/s})^2}{2(9.8 \text{ m/s}^2)}$$

$$h = 5.10 \text{ m}$$

Elastic Potential Energy & Kinetic Energy

MP/292



$$E_{\text{total}} = E'_{\text{total}}$$

(cart) (max compression)

$$E_k + \cancel{E_e} = \cancel{E'_k} + E'_e$$

$$E_k = E'_e$$

$$\cancel{\frac{1}{2}mv^2} = \cancel{\frac{1}{2}kx^2}$$

$$mv^2 = kx^2$$

$$v^2 = \frac{kx^2}{m}$$

$$v^2 = \frac{(155\frac{\text{N}}{\text{m}})(0.060\text{m})^2}{0.25\text{kg}}$$

$$v^2 = 2.232\frac{\text{m}^2}{\text{s}^2}$$

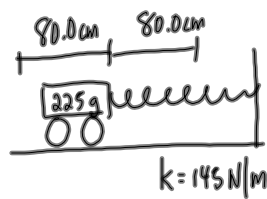
$$v = \pm 1.5\text{ m/s}$$

use the negative
since it
is a
compression

$$v = -1.5\text{ m/s (compression)}$$

(1.5 m/s toward the spring)

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a) $E_{\text{total}} = E'_{\text{total}}$
 (equilib) (max stretch/compress)

$E_e + E_k = E'_e + E'_k$

$\frac{1}{2}mv^2 = \frac{1}{2}kx^2$

$v^2 = \frac{kx^2}{m}$

$v^2 = \frac{(145 \frac{N}{m})(0.800m)^2}{0.225kg}$

$v^2 = 412.4 \frac{m^2}{s^2}$

$v = \pm 20.3 \text{ m/s}$

a) $v_{\text{max}} = ?$

b) $x = ?$ when $\frac{1}{2}v_{\text{max}}$

b) $\frac{1}{2}$ of $v_{\text{max}} = 10.15 \text{ m/s}$

$x = ?$

$E_{\text{total}} = E'_{\text{total}}$
 (equilibrium) (partial stretch)

$E_e + E_k = E'_e + E'_k$

$\frac{1}{2}mv^2 = \frac{1}{2}kx^2 + \frac{1}{2}mv'^2$

$(0.225kg)(20.3 \frac{m}{s})^2 = (145 \frac{N}{m})x^2 + (0.225kg)(10.15 \frac{m}{s})^2$

$92.7 \text{ J} = (145 \frac{N}{m})x^2 + 23.7 \text{ J}$

$69.5 \text{ J} = (145 \frac{N}{m})x^2$

$x^2 = \frac{69.5 \text{ J}}{145 \text{ N/m}}$

$\frac{N \cdot m}{\frac{N}{m}} = \frac{N \cdot m \cdot m}{N} = m^2$

$x^2 = 0.479 \text{ m}^2$

$x = \pm 0.692 \text{ m}$

69.2 cm stretch (+)
 compression (-)

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