

PP/317

27.

+ north

|   | Before            | After              |               |
|---|-------------------|--------------------|---------------|
|   | cannon+ball       | cannon             | ball          |
| m |                   | 1385 kg            | 58.5 kg       |
| v | 0                 | v                  | +49.8 m/s     |
| P | 0                 | (1385 kg)v         | 2913.3 kg·m/s |
|   | $\vec{P}_{total}$ | $\vec{P}'_{total}$ |               |

Law of  
Conservation  
of Momentum

$$\Rightarrow \vec{P}_{total} = \vec{P}'_{total}$$

$$0 = (1385 \text{ kg})v + 2913.3 \text{ kg}\cdot\text{m/s}$$

$$-2913.3 \text{ kg}\cdot\text{m/s} = (1385 \text{ kg})v$$

$$v = -2.10 \text{ m/s}$$

$$\vec{v} = 2.10 \text{ m/s [south]}$$

↑  
recoil velocity of the cannon

Elastic Collisions

This is a special type of collision. An elastic collision occurs when the total kinetic energy before the collision is the same as the total kinetic energy after the collision.

\* Not all collisions are elastic!!

\* All collisions obey the Law of Conservation of Momentum (neglecting friction)

MP/320

|   | Before          |         | After            |            |
|---|-----------------|---------|------------------|------------|
|   | Bill            | Steel   | Bill             | Steel      |
| m | 0.250kg         | 0.800kg | 0.250kg          | 0.800kg    |
| v | +5.00m/s        | 0       | -2.62m/s         | v          |
| P | +1.25<br>kg.m/s | 0       | -0.655<br>kg.m/s | (0.800kg)v |

+ Forward

$\vec{P}_{\text{total}} = \vec{P}'_{\text{total}}$

$$1.25 \text{ kg}\cdot\text{m/s} + 0 = -0.655 \text{ kg}\cdot\text{m/s} + (0.800 \text{ kg})v$$

$$1.905 \text{ kg}\cdot\text{m/s} = (0.800 \text{ kg})v$$

$$v = +2.38 \text{ m/s}$$

$$\vec{v} = 2.38 \text{ m/s [forward]}$$

$E_k$  (before)

$$E_k(\text{Bill}) = \frac{1}{2}(0.250 \text{ kg})(5.00 \text{ m/s})^2 = 3.125 \text{ J}$$

$$E_k(\text{Steel}) = 0$$

$$E_k(\text{total}) = 3.125 \text{ J}$$

or [in the original direction of the billiard ball]

$E_k$  (after)

$$E_k'(\text{Bill}) = \frac{1}{2}(0.250 \text{ kg})(2.62 \text{ m/s})^2 = 0.85805 \text{ J}$$

$$E_k'(\text{Steel}) = \frac{1}{2}(0.800 \text{ kg})(2.38 \text{ m/s})^2 = 2.26576 \text{ J}$$

$$E_k'(\text{total}) = 3.12 \text{ J}$$

Since  $E_k(\text{total}) = E_k'(\text{total})$

the collision was elastic.

TO DO: ① PP/322  
② HW Probe from §7-1